

1 Design of a Friction Clutch Using Dual 2 Belleville Structures

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12 *This paper presents a simplified friction clutch design, which con-*
 13 *sists of the dual Belleville spring and the friction plates. This*
 14 *design exploits the preset angle on the Belleville spring to in-*
 15 *crease the friction area during operation; thus, the load on spring*
 16 *is reduced at a given transmitted torque. Due to the increasing of*
 17 *friction area, the Belleville spring can also act as a friction plate,*
 18 *and the components required for the clutch can be reduced. The*
 19 *maximum transmittable torque of the clutch is easily adjusted by*
 20 *varying the preload on the Belleville spring. Moreover, it is very*
 21 *easy to assemble the components of the present clutch. To demon-*
 22 *strate the present design, a prototype friction clutch with a*
 23 *Belleville spring has been fabricated and tested. We showed that*
 24 *the transmitted torque remained constant for different operating*
 25 *speeds. [DOI: 10.1115/1.2748454]*

26 *Keywords: friction clutch, Belleville spring, coefficient of friction*

27 Introduction

28 The overload protection devices are designed to prevent the
 29 damage of machinery or drive line in the event of an overload or
 30 jamming. The overload protection devices have been extensively
 31 employed in various applications such as automatic screwdrivers,
 32 printers, conveyor belts, and automobile power windows, etc. The
 33 most common overload protection devices are the friction clutches
 34 that adapted to the smooth engagement of shafts with different
 35 angular velocities. The basic operation concept is to force two
 36 opposing surfaces into frictional contact by means of a preset
 37 load. The torque, if it is not overloaded, will be fully transmitted
 38 by the clutch under the assistance of friction force. When the
 39 transmitted torque exceeds the design limit (i.e., overload), the

slip between the two friction surfaces will occur. The clutch will
 no longer fully transmit this overload torque, and will act as an
 overload protection device.

In general, the friction clutches have normally engaged and
 normally disengaged designs. Figure 1 shows a typical normally
 disengaged radial friction clutch that consists of the drive shaft,
 the friction plate (lining), the helical spring, and the driven shaft.
 The torque capacity of friction clutch is the function of clutch
 size, friction coefficient μ , number of friction faces, and axial
 force [1]. When the drive shaft applies a load to the helical spring,
 so as to lead to the contact of friction plates, the power will
 transmit from the drive shaft to the driven shaft. The friction force
 between the friction plates can be adjusted by varying the restor-
 ing force of the helical spring. Thus, the torque allowed to trans-
 mit by this friction clutch is determined. As a second example, the
 drive members and the driven members are normal engaged. The
 friction plates normally make contact with each other except for
 the existence of overload. In [2,3], the Belleville spring (also re-
 ferred to as the conical disk spring) is used to apply an axial load
 to push the friction faces.

The disadvantage of the existing friction clutch is the require-
 ment of various components. In addition, it is time consuming to
 assemble these components. In this study, a normally engaged
 friction clutch has been designed and analyzed, as illustrated in
 Fig. 2. The friction clutch mainly consists of the dual slit
 Belleville spring and lining. These Belleville springs are used to
 generate the friction force of the clutch, so as to further determine
 the maximum torque transmitted by the clutch. Since the
 Belleville spring is stiffer than the helical compression spring, it
 can provide huge force with a small deflection. Moreover, the
 assembly of the present clutch is simple and fast; and its cost can
 be significantly reduced.

Design Concept

The present clutch shown in Fig. 2 employs the restoring force
 of Belleville springs to provide an axial load. Figure 3 shows the
 exploded drawing of the clutch in Fig. 2. The power inputs into
 the mechanism through drive gear (#9), outputs from the mecha-
 nism through the driven gear (#1). The shaft #8 is fixed to gear #9,
 and the friction plates (lining) #6 with four inner anchors are
 locked to the key ways of shaft (#8). Thus, the friction plates and
 shaft are driven by gear #9, and all of these components (named
 the drive set) have the same angular velocity. The Belleville
 springs (#5) and intermediate plate (#7) with four outer anchors
 are fixed to the slots of the driven gear (#1), and all of these three
 components (named the driven set) have the same angular velocity.
 The drive set and the driven set have the same angular velocity
 in normal operation circumstances, whereas these two sets have
 different angular velocities during the overload situation. The
 Belleville springs will apply an adjustable load P on the friction
 plate #6 by varying the position of the nut (#2), so as to further
 induce a friction force between the friction plates and the inter-
 mediate plate. After that, the nut is fastened to the shaft (#8) using
 the setscrew (#3). Thus, the power can transmit from the drive
 gear #9 to the driven gear #1. Moreover, the transmitted power

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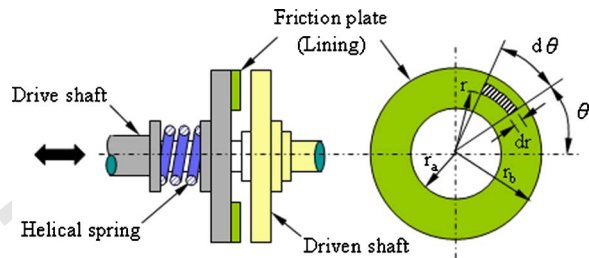


Fig. 1 Schematic of the traditional radian friction clutch

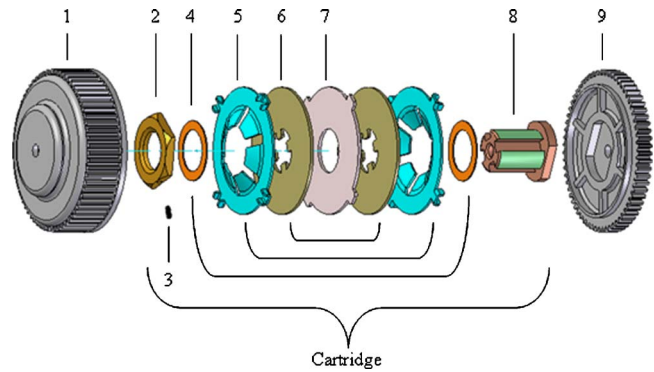


Fig. 3 Key components of the present friction clutch: driven gear (#1), nut (#2), setscrew (#3), washer (#4), Belleville springs (#5), friction plate (lining, #6), intermediate plates (#7), stud (#8), and drive gear (#9)

94 can be tuned by varying the load P . When the friction torque T
 95 induced by the transmitted power exceeds the design limit T_{max} ,
 96 the friction plates will slip and the input power from gear #9 will
 97 no longer transmit to gear #1. Thus, the whole device performs as
 98 an overload clutch. Equation (A1) in Appendix A expresses the
 99 relation of load P and friction torque T [1].

100 Figure 4(a) shows the cross section of the present Belleville
 101 spring, which consists of A (conical disk) and B (lever arm) seg-
 102 ments. As discussed in [4], the load-deflection relation of the
 103 Belleville spring is highly nonlinear for a large deformation. The
 104 buckling of the shell structure, which has similar mechanics be-
 105 havior, has been discussed in [5,6]. The influence of structure
 106 thickness on the stiffness of the Belleville spring has been studied

in [7], and the material nonlinearity effect of conical disk springs 107
 has been analyzed in [8]. In order to design and predict the char- 108
 acteristics of the Belleville spring, a small deformation is required 109
 to assure operation at the linear range. The load-deflection char- 110
 acteristics of the Belleville spring are superposed by both of these 111
 two segments. A more detailed description of the Belleville spring 112
 with a two-segment design is available in Appendix B [9]. The 113
 deformation behaviors of the Belleville spring during loading are 114
 indicated in Fig. 4. The case (I) represents the configuration of 115
 spring with no loading. As the load applied on the spring is in- 116
 creased, the spring will be deformed and the center hole will be 117
 decreased. As depicted in case (II), the angle β will become zero 118
 when a critical load P_c is applied to the spring. Thus, the contact 119
 area of the spring will reach a maximum. As shown in case (III), 120
 the edge of region A could be warped if the applied load is greater 121
 than P_c ; meanwhile, the contact area is decreased. The design and 122
 optimization of Belleville springs have been discussed in [10,11]. 123

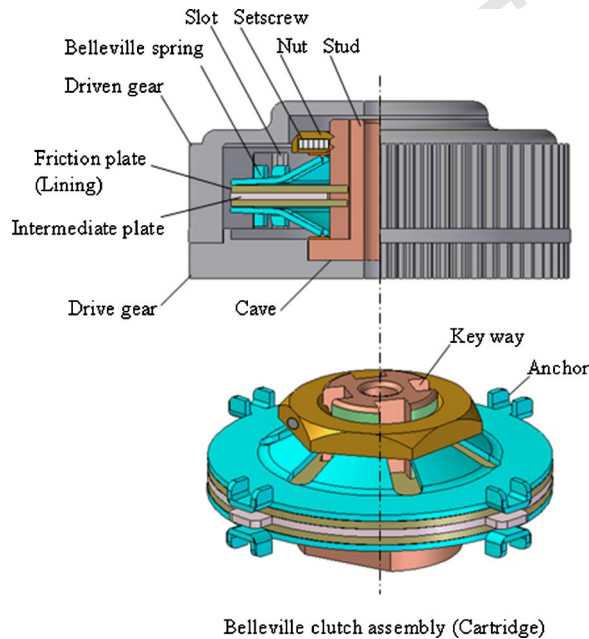


Fig. 2 Schematic of the friction clutch with dual Belleville springs

In summary, the merit of this design is to employ the preset 124
 angle β on the Belleville spring to increase the contact area for 125
 friction at a given preload. According to Eq. (A1), the load P on 126
 the spring can be reduced for a designated transmitted torque. 127
 Moreover, the Belleville structure can act not only as a spring, but 128
 also as a friction plate, and the components required for the clutch 129
 can be reduced. It is possible to tune the mechanical characteris- 130
 tics of the Belleville spring by varying various geometry param- 131
 eters, such as thickness, spring height, angle β , etc. This study 132
 aims to demonstrate the feasibility of applying the Belleville 133
 spring for friction clutch, but not to optimize the design of the 134
 spring. 135

Typical Simulation and Experimental Results 136

This study employed the commercial finite element software 137
 ANSYS to predict the influence of thickness under the similar shape 138

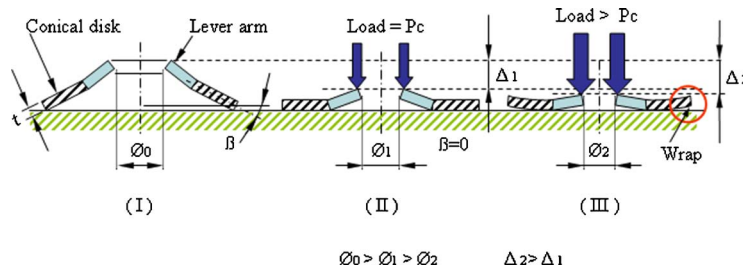


Fig. 4 The characteristics of the Belleville spring under different loads, (I) no loading, (II) maximum contact area under critical loading P_c until $\beta=0$ deg, and (III) the loading over P_c

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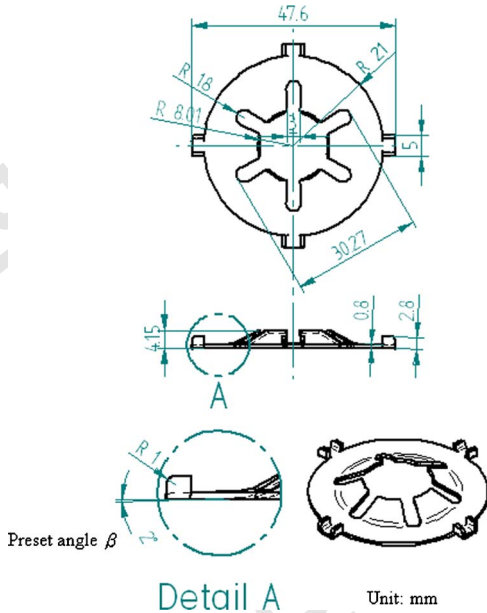


Fig. 5 Dimensions of the prototype Belleville spring for experiment

of the Belleville spring. The dimensions of the Belleville spring established in the finite element model (FEM) are indicated in Fig. 5. In this case, the preset angle β and thickness t of the Belleville spring were in the range $\beta=2-10$ deg, and $t=0.6-1.5$ mm, respectively. Moreover, the element type was SHELL93, and the spring had material constants of Young's modulus $E=200$ GPa and Poisson's ratio $\nu=0.29$. The typical finite element results in Fig. 6(a) show the deflection of the spring with $\beta=2$ deg and thickness $t=0.8$ mm after applying a 185 N load. The slashed line region in Fig. 6(b) summarizes the loads to cause the angle β to become 0 deg for various spring thicknesses ($t=0.6, 0.8, 1.0, 1.2,$ and 1.5 mm) and two preset angles ($\beta=2$ deg and $\beta=10$ deg). Thus, the load can be tuned in the range of 85–4837 N by varying these spring thicknesses and preset angles. These simulation results also point out that the relation between the load and the thickness of spring is nonlinear.

In order to demonstrate the present concept, a prototype friction clutch with a Belleville spring was implemented. Figure 7 demonstrates various key components of the fabricated clutch. As shown in Fig. 7(a), this study selected the SUS304 sheet (surface roughness $PRa=0.346 \mu\text{m}$ measured by Talysurf Series 2) to make the intermediate plate #7 and friction plate #6 using wire electrical discharge machining. The SUS304 material is most widely used for industrial products to offer excellent corrosion resistance [12]. The Belleville spring #5, which demands good formability and strong stiffness, was made of SUP 9 (surface

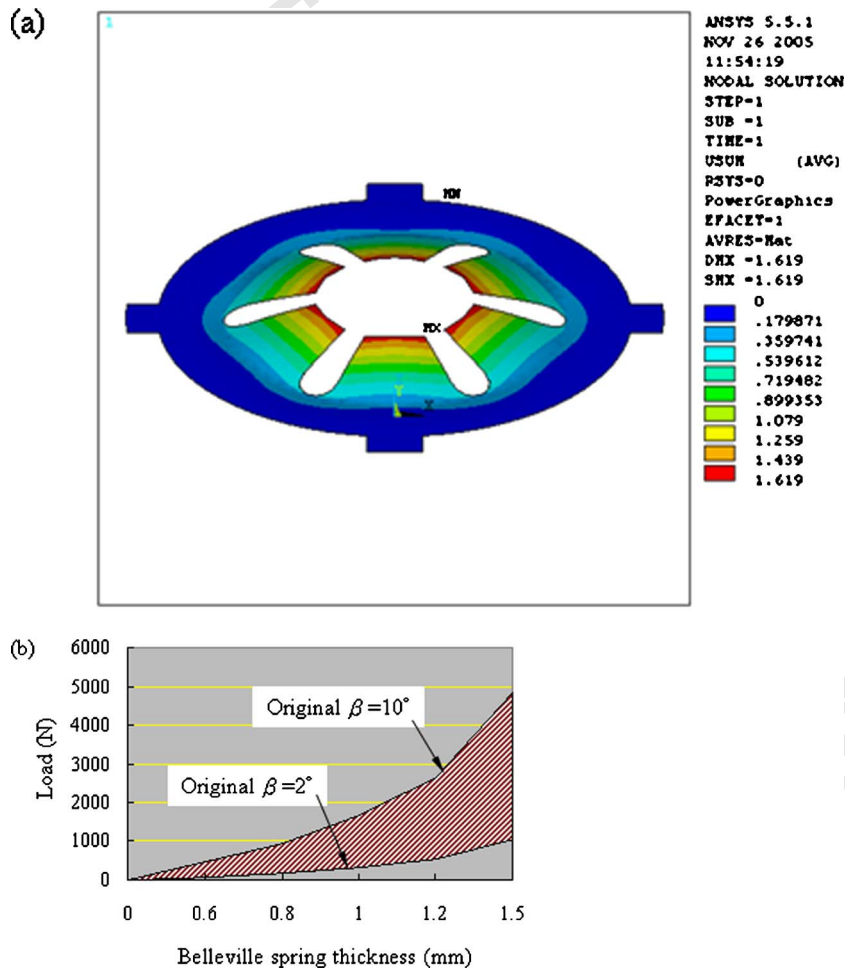


Fig. 6 FEM simulation results (a) typical FEM results when $\beta=2$ deg, $t=0.8$ mm, and preset load of 185 N, and (b) the preset loads required to reach the maximum contact area status in Fig. 4 (II) for different thickness t ($t=0.6, 0.8, 1.0, 1.2,$ and 1.5 mm) and angle β ($\beta=2$ deg and 10 deg)

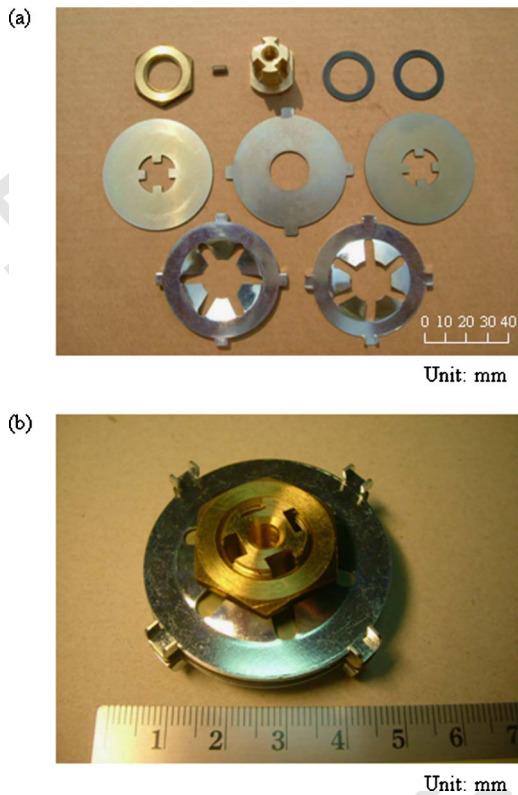


Fig. 7 (a) The fabricated key components of the clutch, and (b) the assembly of the components

165 roughness $PRa=0.5472 \mu\text{m}$). Moreover, the gears #1 and #9 are
 166 made of acetal copolymer by means of the injection-molding pro-
 167 cess. All specimens were inspected and ultrasonically cleaned in
 168 acetone for 10 min after fabrication. The surfaces for friction con-
 169 tact were coated with grease before assembly. Figure 7(b) shows
 170 the assembly of these components.
 171 The experimental setup in Fig. 8 was established to characterize
 172 the performance of the clutch. A DC motor (Mabuchi RS-540)
 173 was employed to move the drive gear (#1); however, the driven
 174 gear (#9) was connected and held by a torque meter (Torqueleader
 175 36/4). Thus, this experiment acted as an overload protection con-

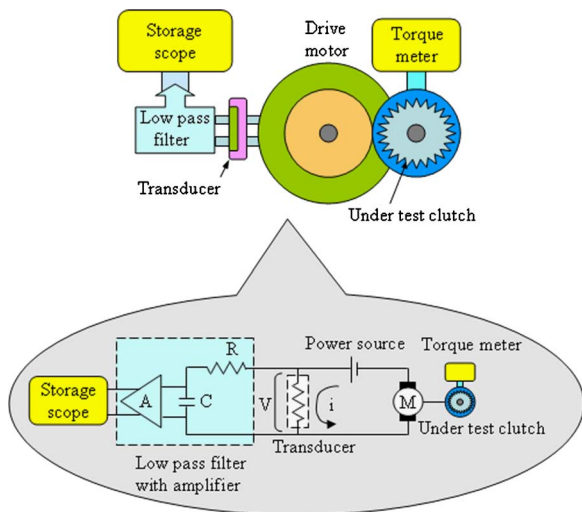


Fig. 8 The experimental setup for the dynamic spinning test of the clutch

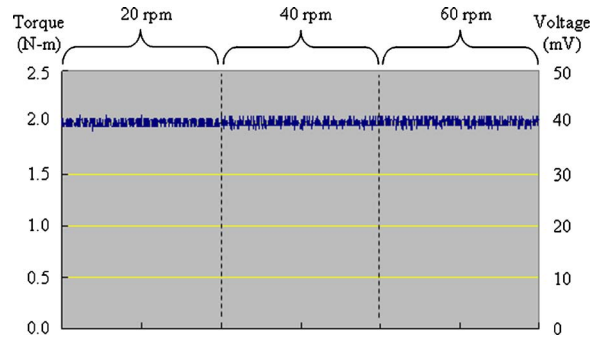


Fig. 9 The torque was close to the preset value of 2 N m for three different operating velocities (20, 40, and 60 RPM)

176 dition, and the relative angular velocity between the gears #1 and
 177 #9 was determined by the DC motor. Thus, the output torque
 178 applied on the shaft was determined. A current/voltage
 179 (50 A/50 mV) transducer (Lutron ST-50) was used to measure
 180 the motor armature current. A low-pass filter and an amplifier
 181 (amplification gain=1000) were used to reduce the noise during
 182 measurement. The resistance and capacitance were $R=28 \text{ ohm}$
 183 and $C=47 \mu\text{f}$, respectively, and the cut-off frequency was
 184 $f_c \approx 120 \text{ Hz}$. During the test, the nut #2 was adjusted to give the
 185 T_{max} of 2 N m. The DC motor had three different angular speeds
 186 (20, 40, and 60 RPM) to demonstrate the performance of clutch at
 187 different relative angular velocity of gear #1 and gear #9. The
 188 measurement results in Fig. 9 shows that the torque was close to
 189 the preset value of 2 N m for these three angular velocities (20,
 190 40, and 60 RPM), even though the original torque remained the
 191 same after 1000 cycles of operation.

Conclusions

192
 193 The study has presented a novel friction clutch using the
 194 Belleville spring as the key component. This design exploits the
 195 preset angle β on the Belleville spring to increase the friction area
 196 during operation; thus, the load P on spring is reduced at a given
 197 transmitted torque. Due to the increasing of friction area, the
 198 Belleville spring can also act as a friction plate, and the compo-
 199 nents required for the clutch can be reduced. The allowable trans-
 200 mitted torque is adjusted by tuning the predeformation of the
 201 Belleville spring. Once the transmitted torque exceeds the friction
 202 torque preset by the restoring force of the Belleville spring, the
 203 friction plates and the intermediate plate will slip, so as to perform
 204 as an overload clutch. In application, a friction clutch with a
 205 Belleville spring has been fabricated and tested. The measurement
 206 results demonstrated that the mechanism did act as an overload
 207 friction clutch; the transmitted torque was close to a preset value
 208 of 2 N m for three different angular velocities, including 20, 40,
 209 and 60 rpm. Thus, various torque requirements for different appli-
 210 cations can easily be satisfied. To enhance the reliability of the
 211 clutch, the problem relating to the temperature rise and wear can
 212 be improved by adding the lubrication grease. Moreover, it is easy
 213 to assemble the present clutch so as to minimize required space as
 214 well as the cost. The basic ideas of this study are applicable to any
 215 situation while overload exists, such as tension on paper, wire
 216 film, and a power window on a vehicle.

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217
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 219 tom Manufacturing Co., Ltd., Taiwan for providing experimental
 220 facilities.

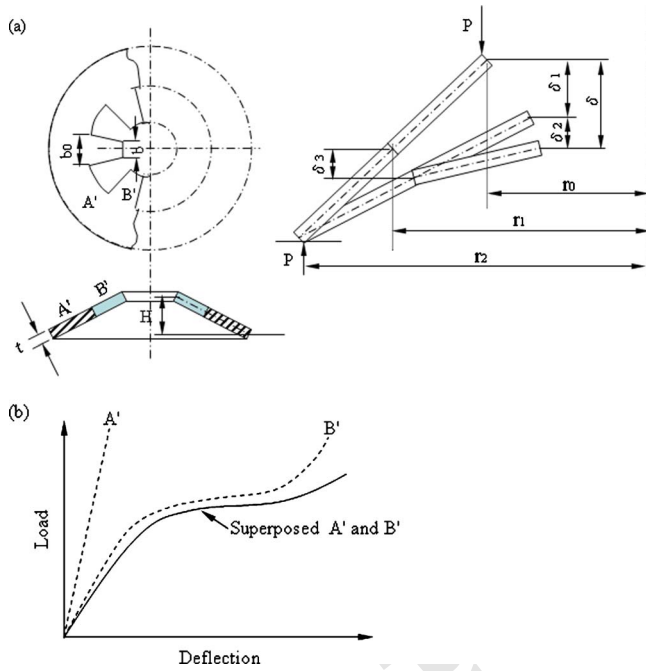


Fig. 10 (a) Schematic of the Belleville spring model, and (b) variation of the load and the deflection δ

$$P = \frac{r_2 - r_1}{r_2 - r_0} \frac{C_1 C_2 E t^4}{r_2^2} \quad (B1) \quad 241$$

where r_0 =inner radii of Belleville spring, r_1 =radii of slit outer Belleville spring edge, r_2 =radii of Belleville spring outer edge, E =Young's module of materials, t =thickness, and the constants C_1 and C_2 are expressed as

$$C_1 = \left(\frac{\alpha + 1}{\alpha - 1} - \frac{2}{\log \alpha} \right) \pi \left(\frac{\alpha}{\alpha - 1} \right)^2 \quad (B2) \quad 246$$

$$C_2 = \frac{\delta_3}{(1 - \nu^2)t} \left[\left(\frac{H - \delta_3}{t} \right) \left(\frac{H - \delta_3}{t} - \frac{\delta_3}{2t} \right) + 1 \right] \quad (B3) \quad 247$$

where H =free height minus thickness, ν =Poisson's ratio, α =radius ratio, r_2/r_1 , and $\delta_1 - \delta_3$ are deflections of the Belleville spring, which can be further expressed as

$$\delta_1 = \delta_3 \frac{r_2 - r_0}{r_2 - r_1} \quad (B4) \quad 251$$

$$\delta_2 = K \frac{4P(r_1 - r_0)^3}{Eb_0 t^3 m} (1 - \nu^2) \quad (B5) \quad 252$$

where b =width of slit tip, b_0 =width of slit datum, m =number of slits, and the constant K is

$$K = \frac{3}{(1 - b/b_0)^3} \left[\frac{1}{2} - 2 \left(\frac{b}{b_0} \right) + \left(\frac{b}{b_0} \right)^2 \left(\frac{3}{2} - \log_{10} \frac{b}{b_0} \right) \right] \quad (B6) \quad 255$$

According to Eqs. (B1)–(B6) the nonlinear load-deflection curves shown in Fig. 10(b) are obtained.

221 **Appendix A: Disk Clutch Torque**

222 The slip friction type clutches consist of one or more friction
223 disks. As shown in Fig. 1, the torque capacity T at an axial clamp-
224 ing force P is expressed as [1],

$$225 \quad T = NP\mu R_f, \quad (A1)$$

226 where μ is the constant friction coefficient, and N is the number of
227 contact surface. In addition, the friction radius R_f is

$$228 \quad R_f = \frac{2}{3} \left(\frac{r_b^3 - r_a^3}{r_b^2 - r_a^2} \right) \quad (A2)$$

229 where r_a and r_b are the inner radii and outer radii, respectively, of
230 the friction plate shown in Fig. 1. Equation (A2) is appropriate for
231 a brand new clutch. However, after the uniform wear takes place,
232 the friction radius R_f becomes

$$233 \quad R_f = \frac{r_b + r_a}{2} \quad (A3)$$

234 According to Eq. (A1), the torque capacity of a clutch increases
235 with the area of friction surface.

236 **Appendix B: Belleville Spring Structure Load-
237 Deflection Characteristics**

238 The slit Belleville spring design formula has been studied in [9]
239 to show the relation of spring features and stiffness. As shown in
240 Fig. 10(a), the relationship between the load P and the spring is

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AUTHOR QUERIES — 011709JMD

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there are separate variables, make them italic.

#2 AQ: If PRa is an acronym, please define. If

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